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# CONSTRUCTION OF REGIONAL TRADE-LINKED SUPPLY AND USE TABLES FOR THE EU28

Description of the methodology

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# 1 Introduction

Economic development is interregional in nature. Physical and technological proximity determined by inter-regional and national cross-border interactions in trade, investments and knowledge are important determinants of economic growth. However, quantitative policy research analysing regional development in Europe taking interregional interactions into account and such as proposed in the regional smart specialization strategy (McCann and Ortega-Argilés, 2012) has been hampered by data deficiencies.

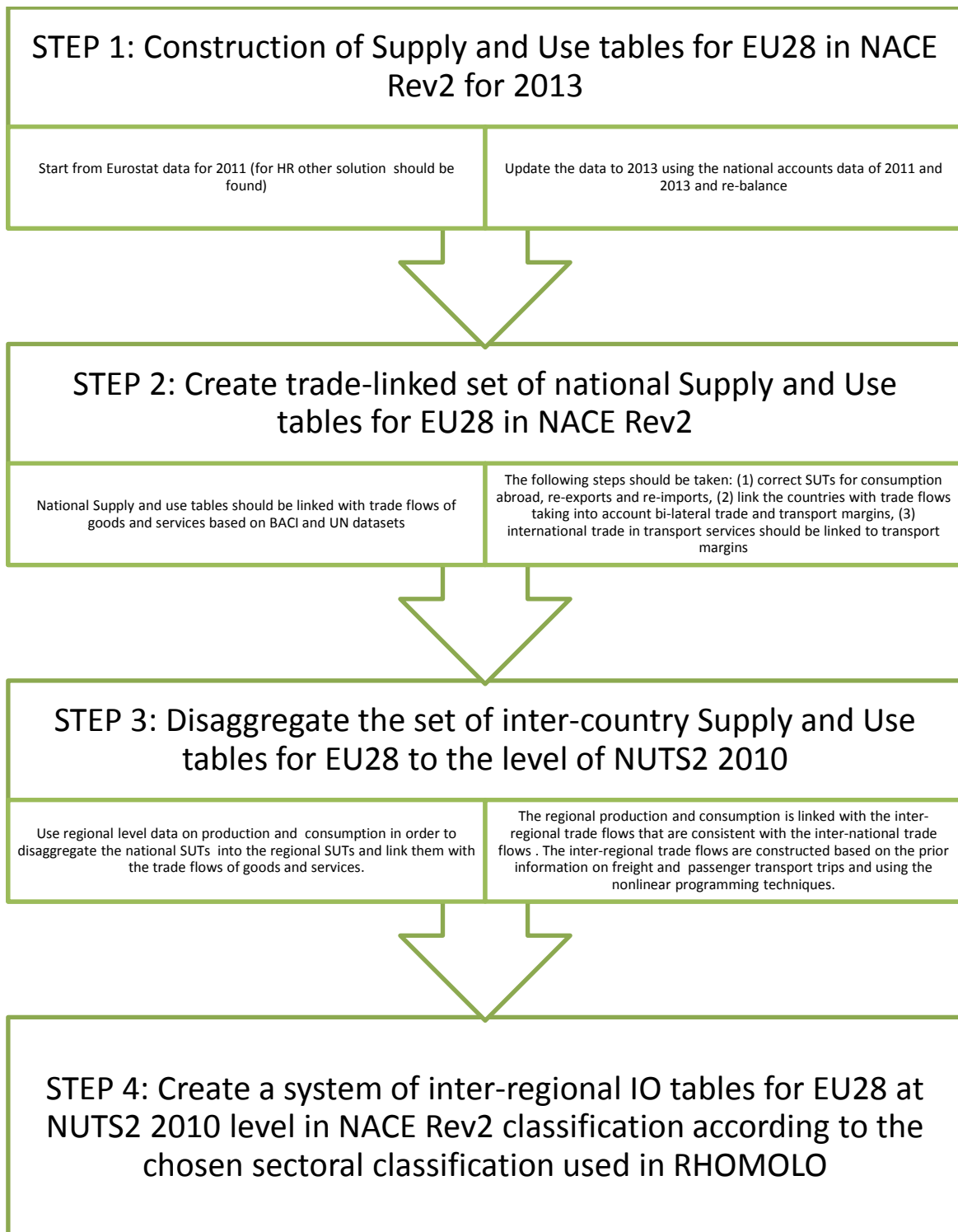
Existing data on inter-regional trade are incomplete and based on data points which are far in the past. Moreover, they cannot be used for modelling purposes since they are estimated themselves using behavioural equations. In addition, they are often based on outdated methodologies are out of line with the structure and empirical evidence underlying the model. Instead, interregional trade flows should be estimated based on the state of the art methodology and developed in such a way that the data can subsequently be used in economic, econometric and spatial CGE analysis.

We implement a methodology for estimating a system of regional supply and use tables consistent with interregional trade data. Trade in goods and services will be derived from freight transport data, airline data on flights and business travel data taking transshipment locations into account. The methodology is centred on the probability of trade flows and is developed to fit the information available, without pre-imposing any geographical structure on the data. The method extends the approach proposed in Thissen et al. (2013) and it is in line with 'parameter-free' universal methodologies as proposed by Simini et al. (2012), making it possible to analyse the importance of transshipment locations (hubs) in regional trade and linking up transport costs to inter-regional trade flows.

In this paper we describe the methodology used to regionalize the supply and Use tables for the EU28 and how we subsequently construct a multiregional product by product IO table. The product by product IO table is constructed on the 2 digit based classification of industries (NACE 2.0) used in the national accounts of Eurostat. In a first step the national supply and use tables are disaggregated into regional supply and use tables based on regional statistics that can be obtained from Eurostat. These "regionalized" supply and use tables, however, are not disaggregated with respect to the interregional and international trade. The interregional and international trade in goods is determined in a second step based on regional transport flows of goods. Interregional trade in services is derived by business trips between regions. The estimation methodology simultaneously estimates the trade and transport flows between regions where different modalities have been taken into account for the transport flows.

Figure 1 represents the main steps in the construction of the Multi-Regional Input-Output (MRIO) table for EU28 at NUTS2 level. The first chapter describes the first two steps towards the construction of the consistent inter-regional MRIO table for EU28, including the update of the existing Eurostat Supply and Use tables in NACE Rev2 classification to the year 2013 and creating trade-linked country-level Supply and Use tables for EU28 and the rest of the world. The second chapter describes the third step, while the creation of an IO table is discussed in chapter 3. The fourth chapter discusses the importance of the used methodology to estimate the regional trade data if compared to existing gravity based estimation methods.

**Figure 1 Schematic data flows for the construction of the inter-regional trade data:**



# 2 National Trade linked Supply and Use Tables

We have to create a set of national supply and use tables that are internally consistent. That is all tables should be trade linked with consistent import and export trade flows between the countries. We start with an overview of available sources of SUTs and IO table that are used. Subsequently we turn to the adjustments that that have to be made to be create an internally consistent international system of SUTs.

## 2.1 Overview of available data sources

Main data sources for the construction of trade-linked Supply and Use tables covering EU28 countries separately as well as the rest of the world include:

1. Data on Supply and Use tables (SUTs) or Input-Output tables (IOs) of the individual countries
2. National accounts data that is used to update SUTs and IOs to the year 2013
3. International trade data for both goods and services

Table 1 below gives an overview of the available data sources used for the construction of the national level trade-linked Supply and Use tables (SUTs). The SUTs and national accounts were collected from Eurostat and OECD publicly accessible databases. International trade data were collected from the BACI database of CEPII and UN trade in services database. Access to the BACI database requires subscription to UN COMTRADE as it is based on this data.

SUTs for EU28 countries in the NACE Revision 2 classification of economic activities<sup>1</sup> are available for different years and are all updated to 2013 using time-series data from national accounts. The SUTs are linked with the international trade flows based on the trade patters from BACI and UN trade in services databases.

**Table 1: Overview of the data sources and their short description**

Data source	Availability	Sectoral/commodity details	Geographical details	Notes
Eurostat National SUTs	2008-2011	NACE Rev2	EU27 (except Croatia)	2013 data is only available for 3 countries No data for Croatia
Eurostat national accounts annual data (main GDP categories)	2000-2015	SNA categories	EU28	

<sup>1</sup> Please see the following document for a description of the NACE classification in economic activities:  
[https://ec.europa.eu/eurostat/statistics-explained/index.php/Glossary:Statistical\\_classification\\_of\\_economic\\_activities\\_in\\_the\\_European\\_Community\\_\(NACE\)](https://ec.europa.eu/eurostat/statistics-explained/index.php/Glossary:Statistical_classification_of_economic_activities_in_the_European_Community_(NACE))



Eurostat national accounts annual data (detailed sectoral split)	2000-2013	90 NACE Rev2 economic sectors	EU28	Some of the sectors are the aggregates of the sub-sectors
BACI international reconciled bi-lateral commodity trade dataset	2008-2014	HS07	232 countries of the world	Represents the reconciled version of UN COMTRADE dataset prepared by CEPII for DG Trade  Trade flows are represented in volumes and in values
STAN database national IO tables	1995-2011	34 sectors/commodities	Croatia and other 63 countries of the world including rest of the world	There is also inter-country IO tables available from OECD that link all countries with trade of goods and services
UN trade in services database	2000-2014	184 types of EBOPS Items (types of services)	260 countries of the world	This database is not reconciled and has relatively a lot of missing values

### 2.1.1 National Supply and Use tables from Eurostat

Eurostat provides Supply and Use tables for all EU28 member states except for Croatia<sup>2</sup>. These tables are produced using NACE Rev2 sectoral and commodity classification and available for various years. The latest year of availability for each of EU28 countries is presented in the table below. Countries with the most recent data (that is the data for 2011 and 2012) are Czech Republic, Finland, Luxembourg and United Kingdom. Supply and Use tables from Eurostat are unbalanced for many countries after updating, they include re-exports and re-imports and, in some cases, the fixed capital formation column contains negative elements. We need a consistent set of trade linked SUTs before we can start the regionalisation. In a first step we therefore make the SUTs consistent after which we will continue with the linking of the SUTs by international trade flows.

The fact that the SUTs from Eurostat are not available for the year 2013 for any of the EU28 countries means that we would need to use growth rates based on the national accounts data in order to project the tables to 2013.

**Table 2: Overview of data availability for Supply and Use tables in NACE Rev2 at Eurostat**

Country	Data type	Last available year
AT Austria	Supply and Use tables in NACE Rev2	2010
BE Belgium	Supply and Use tables in NACE Rev2	2010
BG Bulgaria	Supply and Use tables in NACE Rev2	2010
CY Cyprus	Supply and Use tables in NACE Rev2	2009

<sup>2</sup> For Croatia we have used the dataset received from IPTS.

CZ Czech Republic	Supply and Use tables in NACE Rev2	2011
DE Germany	Supply and Use tables in NACE Rev2	2010
DK Denmark	Supply and Use tables in NACE Rev2	2009
EE Estonia	Supply and Use tables in NACE Rev2	2009
ES Spain	Supply and Use tables in NACE Rev2	2010
FI Finland	Supply and Use tables in NACE Rev2	2011
FR France	Supply and Use tables in NACE Rev2	2010
GR Greece	Supply and Use tables in NACE Rev2	2010
HU Hungary	Supply and Use tables in NACE Rev2	2010
IE Ireland	Supply and Use tables in NACE Rev2	2010
IT Italy	Supply and Use tables in NACE Rev2	2010
LT Lithuania	Supply and Use tables in NACE Rev2	2010
LU Luxembourg	Supply and Use tables in NACE Rev2	2012
LV Latvia	Supply and Use tables in NACE Rev2	2010
MT Malta	Supply and Use tables in NACE Rev2	2010
NL Netherlands	Supply and Use tables in NACE Rev2	2010
PL Poland	Supply and Use tables in NACE Rev2	2009
PT Portugal	Supply and Use tables in NACE Rev2	2008
RO Romania	Supply and Use tables in NACE Rev2	2010
SE Sweden	Supply and Use tables in NACE Rev2	2010
SI Slovenia	Supply and Use tables in NACE Rev2	2010
SK Slovakia	Supply and Use tables in NACE Rev2	2010
UK United Kingdom	Supply and Use tables in NACE Rev2	2011

### 2.1.2 National accounts data from Eurostat

For the period 2005 to 2014 Eurostat provides national accounts of all EU28 countries covering many of the same elements as the national Supply and Use tables. This includes all elements of final consumption (final consumption of households, final consumption of NPISH, final consumption of government, fixed capital formation and changes in inventories), exports and imports. The data is however not split between the economic sectors but could still be used to create homogenous growth rates for the respective parts of the SUTs. Table 3 below presents the full list of national accounts data elements provided by Eurostat and used to project the SUTs to the year 2013.

**Table 3: The list of national accounts elements**

B1GQ	Gross domestic product at market prices
B1G	Value added, gross
P3	Final consumption expenditure
P3_S13	Final consumption expenditure of general government
P31_S13	Individual consumption expenditure of general government
P32_S13	Collective consumption expenditure of general government
P31_S14_S15	Household and NPISH final consumption expenditure
P31_S14	Final consumption expenditure of households
P31_S15	Final consumption expenditure of NPISH
P41	Actual individual consumption
P5G	Gross capital formation
P51G	Gross fixed capital formation
P52_P53	Changes in inventories and acquisitions less disposals of valuables
P52	Changes in inventories
P53	Acquisitions less disposals of valuables
P6	Exports of goods and services
P61	Exports of goods
P62	Exports of services
P7	Imports of goods and services

P71	Imports of goods
P72	Imports of services
B11	External balance of goods and services
B111	External balance - Goods
B112	External balance - Services
D1	Compensation of employees
D11	Wages and salaries
D12	Employers' social contributions
B2A3G	Operating surplus and mixed income, gross
D2X3	Taxes on production and imports less subsidies
D2	Taxes on production and imports
D3	Subsidies
D21X31	Taxes less subsidies on products
D21	Taxes on products
D31	Subsidies on products
YA1	Statistical discrepancy (production approach)
YA0	Statistical discrepancy (expenditure approach)
YA2	Statistical discrepancy (income approach)
P3_P5	Final consumption expenditure and gross capital formation
P3_P6	Final consumption expenditure, gross capital formation and exports of goods and services

Besides the aggregated national accounts data, Eurostat also provides detailed sectoral data for the period 2005-2014 in NACE Rev2 classification (the same 64 sectors as used in SUTs). This data includes:

- Gross value added
- Wages
- Output
- Net operate surplus
- Net taxes minus subsidies on production

These data were also used in order to construct growth rates capturing changes in the economic structure of the EU28 countries and update the sectoral detail of the SUTs to the year 2013.

### 2.1.3 Data for the rest of the world from OECD

Supply and use tables for non-European countries come from the OECD world-wide Input-Output database for 2011. These SUTs are derived from IO tables and hence have diagonal supply tables.

The sectoral classification chosen by OECD for its input-output database is slightly different from NACE Rev2 and includes 34 economic sectors presented in the table below.

**Table 4 List of the sectors/commodities used in OECD Input-Output database**

1	TTL_C01T05: Agriculture, hunting, forestry and fishing
2	TTL_C10T14: Mining and quarrying
3	TTL_C15T16: Food products, beverages and tobacco
4	TTL_C17T19: Textiles, textile products, leather and footwear
5	TTL_C20: Wood and products of wood and cork
6	TTL_C21T22: Pulp, paper, paper products, printing and publishing
7	TTL_C23: Coke, refined petroleum products and nuclear fuel
8	TTL_C24: Chemicals and chemical products
9	TTL_C25: Rubber and plastics products
10	TTL_C26: Other non-metallic mineral products
11	TTL_C27: Basic metals
12	TTL_C28: Fabricated metal products
13	TTL_C29: Machinery and equipment, nec
14	TTL_C30T33X: Computer, Electronic and optical equipment
15	TTL_C31: Electrical machinery and apparatus, nec

16	TTL_C34: Motor vehicles, trailers and semi-trailers
17	TTL_C35: Other transport equipment
18	TTL_C36T37: Manufacturing nec; recycling
19	TTL_C40T41: Electricity, gas and water supply
20	TTL_C45: Construction
21	TTL_C50T52: Wholesale and retail trade; repairs
22	TTL_C55: Hotels and restaurants
23	TTL_C60T63: Transport and storage
24	TTL_C64: Post and telecommunications
25	TTL_C65T67: Financial intermediation
26	TTL_C70: Real estate activities
27	TTL_C71: Renting of machinery and equipment
28	TTL_C72: Computer and related activities
29	TTL_C73T74: R&D and other business activities
30	TTL_C75: Public administration and defence; compulsory social security
31	TTL_C80: Education
32	TTL_C85: Health and social work
33	TTL_C90T93: Other community, social and personal services
34	TTL_C95: Private households with employed persons

The OECD input-output database covers the whole world and includes the data on 62 separate countries and the rest of the world is aggregated in one remaining rest of the world region.

Besides the data on the input-output tables for various countries of the world and the rest of the world region, OECD provides time-series data for the aggregated elements of the national accounts of 42 of the countries presented in its input-output database which make it possible to project IO tables for different years.

#### 2.1.4 International trade data

The international trade in goods data was taken from the BACI international trade database which which reconciles UN data and covers more than 200 countries and 5,000 products, between 1994 and 2014. The Trade in Services was taken from the UN trade in services database Database on annual bilateral services trade flows for 199 countries from 1985 to 2011 that follow the guidelines from the associated UN trade in services report (<http://unstats.un.org/unsd/statcom/doc04/trade-in-services.pdf>). The Table below presents the sectoral coverage of the trade in services database.

**Table 5 List of the types of services in UN trade in services database**

1 Transportation	5 Insurance services
1.1 Sea transport	5.1 Life insurance and pension funding
1.1.1 Passenger	5.2 Freight insurance
1.1.2 Freight	5.3 Other direct insurance
1.1.3 Other	5.4 Reinsurance
1.2 Air transport	5.5 Auxiliary services
1.2.1 Passenger	6 Financial services
1.2.2 Freight	7 Computer and information services
1.2.3 Other	7.1 Computer services
1.3 Other transport	7.2 Information services
1.3.1 Passenger	7.2.1 News agency services
1.3.2 Freight	7.2.2 Other information provision services
1.3.3 Other	8 Royalties and license fees
1.4 Other transport of which: Space transport	8.1 Franchises and similar rights
1.5 Other transport of which: Rail transport	8.2 Other royalties and license fees
1.5.1 Passenger	9 Other business services

1.5.2 Freight	9.1 Merchanting and other trade-related services
1.5.3 Other	9.1.1 Merchanting
1.6 Other transport of which: Road transport	9.1.2 Other trade-related services
1.6.1 Passenger	9.2 Operational leasing services
1.6.2 Freight	9.3 Miscellaneous business, professional, and technical services
1.6.3 Other	9.3.1 Legal, accounting, management consulting, and public relations
1.7 Other transport of which: Inland waterway transport	9.3.1.1 Legal services
1.7.1 Passenger	9.3.1.2 Accounting, auditing, bookkeeping, and tax consulting services
1.7.2 Freight	9.3.1.3 Business and management consulting and public relations services
1.7.3 Other	9.3.2 Advertising, market research, and public opinion polling
1.8 Other transport of which: Pipeline transport and electricity transmission	9.3.3 Research and development
1.9 Other transport of which: Other supporting and auxiliary transport services	9.3.4 Architectural, engineering, and other technical services
2 Travel	9.3.5 Agricultural, mining, and on-site processing services
2.1 Business travel	9.3.5.1 Waste treatment and depollution
2.1.1 Expenditure by seasonal and border workers	9.3.5.2 Agricultural, mining, and other on-site processing services
2.1.2 Other	9.3.6 Other business services
2.2 Personal travel	9.3.7 Services between related enterprises, n.i.e.
2.2.1 Health-related expenditure	10 Personal, cultural, and recreational services
2.2.2 Education-related expenditure	10.1 Audio-visual and related services
2.2.3 Other	10.2 Other personal, cultural, and recreational services
3 Communications services	10.2.1 Education services
3.1 Postal and courier services	10.2.2 Health services
3.1.1 Postal services	10.2.3 Other
3.1.2 Courier services	11 Government services, n.i.e.
3.2 Telecommunications services	11.1 Embassies and consulates
4 Construction services	11.2 Military units and agencies
4.1 Construction abroad	11.3 Other government services
4.2 Construction in the compiling economy	

## 2.2 Updating Eurostat Supply and Use tables for EU28 to 2013

Before upscaling the Eurostat Supply and Use table to the year 2013, it is necessary to check the data for strange values and inconsistencies. Only after we have consistent and correct tables we can link the trade flows between the Eurostat table for Europe and the OECD tables.

### 2.2.1 Upscaling Eurostat Supply and Use tables using national accounts data

The following checks have been performed:

1. Check that for all EU28 countries there is data available from SUTs on wages, fixed capital formation and net operative surplus. For some EU countries this type of data is missing and we need to create for them the missing data using the EU average data on sector-specific ratios.
2. Check for the mismatch between supply and use from SUTs for a specific product group. In case of such mismatch the corresponding rows and columns of SUTs have been removed.
3. Check for the negative values in fixed capital formation column of the use table and replace the negative values with the positive ones on the basis of EU average ratios of fixed capital formation to total supply.

In order to simplify the trade linking of the SUTs of various EU28 countries we move the data for 'Direct purchases abroad by residents' to the households' consumption column of the use table and the data for 'Purchases on the domestic territory by non-residents' to the exports column of the use table. We use the structure of respectively households' consumption and exports in order to split the values between different commodity groups.

Various elements of the cleaned SUTs from Eurostat have been further scaled up with the different elements of the national accounts data. The table below presents the correspondence between the elements of SUTs and the growth rates between the last available year and 2013 from the national accounts.

**Table 6 Correspondence between the elements of SUTs and growth rates based on the national accounts data**

Element of SUTs	Element of national accounts data
Sectoral outputs and inputs	Sectoral outputs
Sectoral wages	Sectoral wages
Sectoral net operative surplus	Sectoral net operative surplus
Consumption of fixed capital by sector	Sectoral outputs
Sectoral net taxes on production	Sectoral net taxes on production
Households consumption by type of commodity	Households consumption total
NIPSH consumption by type of commodity	NIPSH consumption total
Governmental consumption by type of commodity	Governmental consumption total
Fixed capital formation by type of commodity	Fixed capital formation total
Exports by type of commodity	Exports total
Imports by type of commodity	Imports total
All remaining elements	GDP

### 2.2.2 Balancing Supply and Use tables for 2013

Both the initial SUTs from Eurostat as well as the SUTs with the growth rates to the year 2013 are unbalanced. This means that supply and demand for particular types of commodities are not equal and that zero profit condition does not hold for the economic sectors. For the use in the project and the RHOMOLO model SUTs for EU28 countries should be consistent and balanced. For the balancing of SUTs we use the nonlinear programming method where we minimize the measure of distance between the initial updated SUTs and the resulting balanced SUTs under a set of constraints.

The set of constraints includes the following:

1. Supply is equal demand for all commodities
2. Zero profit condition holds for all economic sectors
3. GDP calculated from the SUTs is consistent with the Eurostat data from 2013
4. Transport and trade margins are balanced (sum of positive elements of the column is equal to the sum of negative elements of the column)
5. There are no re-exports (output time EU-average export rate is not lower than the exports)
6. There are no re-imports (total consumption is lower than the imports)
7. Net taxes on consumption commodities cannot be larger than 90% of the value of the total consumption
8. Zero elements of the SUTs should stay equal to zero
9. The variation of the results of the nonlinear programming problem should not exceed 25% of the initial value of the SUTs. This restriction is implemented via introduction of lower and upper boundaries for the outputs of the nonlinear programming problem.

The full formulation of the nonlinear programming problem is presented below. The nonlinear programming problem is solved separately for each country of EU28.

Indexes are defined as:

- *cnt* index for the countries
- *s* index for the economic sectors
- *p* index for the commodities
- *c* index for columns of SUTs
- *r* index for rows of SUTs
- 'P7' Imports CIF
- 'P118' Trade and transport margins
- 'D21\_M\_D31' Taxes less subsidies on products
- 'P6' Exports FOB
- *fdem* Subset of final demand categories
- *vadded\_f* Subset for value added categories

Variables are defined as:

- $SUP_{cnt,r,c}$  supply table
- $USE_{cnt,r,c}$  use table

Parameters are defined as:

- $SUP_{cnt,r,c}$  initial data for supply table
- $USE_{cnt,r,c}$  initial data for use table

Finally, equations are defined as:

- Supply is equal to demand for all commodities:

$$\sum_c SUP_{-v_{cnt,p,c}} = \sum_c USE_{-v_{cnt,p,c}} \quad (1)$$

- Zero profit condition holds for all the economic sectors:

$$\sum_r SUP_{-v_{cnt,r,s}} = \sum_r USE_{-v_{cnt,r,s}} \quad (2)$$

- GDP calculated from SUTs should be consistent with the GDP reported by Eurostat for 2013:

$$GDP_{2013} = \sum_{p,s} SUP_{-v_{cnt,p,s}} - \sum_{p,s} USE_{-v_{cnt,p,p}} + \sum_p USE_{-v_{cnt,p,'D21\_M\_D31'}} \quad (3)$$

- No re-exports, the domestic output times the EU28 average share that goes to exports should not be lower than exports of the country:

$$\sum_s SUP_{-v_{cnt,p,s}} \cdot (1 - Dom\_cons_p) \geq SUP_{-v_{cnt,p,'P7'}} \quad (4)$$

- No re-imports, the value of net total consumption in the country is not lower than the imports of the country:

$$\sum_s USE_{-v_{cnt,p,s}} + \sum_{c \in fdem} USE_{-v_{cnt,p,c}} - SUP_{-v_{cnt,p,'P118'}} \geq SUP_{-v_{cnt,p,'P7'}} \quad (5)$$

- The value of total consumption per type of commodity times 0.9 is not lower than the value of the transport and trade margins plus the net taxes on consumption:

$$\left( \sum_s USE_{-v_{cnt,p,s}} + \sum_{c \in fdem} USE_{-v_{cnt,p,c}} - (SUP_{-v_{cnt,p,'P118'}})_{SUP_{-v_{cnt,p,'P118'}} \leq 0} \right) \cdot 0.9 \geq (SUP_{-v_{cnt,p,'P118'}})_{SUP_{-v_{cnt,p,'P118'}} \geq 0} + SUP_{-v_{cnt,p,'D21\_M\_D31'}} \quad (6)$$

- The optimization function is the entropy function that measures the distance between the initial called SUTs and the outcome of the nonlinear programming program:

$$\begin{aligned} & \sum_{p,s} abs(USE_{-v_{cnt,p,s}}) \cdot \log(abs(USE_{-v_{cnt,p,s}}) / abs(USE_{cnt,p,s})) \\ & + \sum_{p,c} abs(USE_{-v_{cnt,p,c}}) \cdot \log(abs(USE_{-v_{cnt,p,c}}) / abs(USE_{cnt,p,c})) \\ & + \sum_{r \in vadded\_f,s} abs(SUP_{-v_{cnt,r,s}}) \cdot \log(abs(SUP_{-v_{cnt,r,s}}) / abs(SUP_{cnt,r,s})) \rightarrow \min \end{aligned} \quad (7)$$



## 2.3 Preparing the data of the rest of the world

### 2.3.1 Upscaling and balancing OECD Supply and Use tables to 2013 using national accounts data

The data from OECD is provided in the form of IO tables for on 62 separate countries (all EU28 member states are presented as well) and one aggregated rest of the world region. The latest database of the OECD is constructed for the year 2011 and should be scaled up to the year 2013 for the use in the project. National accounts data from OECD is not as detailed as the one from Eurostat and we can only use the growth rates for the GDP as a whole in order to scale the data to 2013. The data from OECD contains some strange values that need to be removed and modified and there are many missing values in the value-added part of the IO table. The strange values include for example the negatives for fixed capital formation, exports and imports. The missing parts of the value-added include consumption of fixed capital and net operative surplus by economic sector.

In the same way as in case of the Eurostat tables we move the data for 'Direct purchases abroad by residents' to the households' consumption column of the use table and the data for 'Purchases on the domestic territory by non-residents' to the exports column of the use table. We use the structure of respectively consumption of the final consumer (there is only one category in the OECD IO tables) and exports in order to split the values between different commodity groups.

The initial OECD IO tables are unbalanced and include re-exports and re-imports for some countries. These re-exports and re-imports should be removed and IO tables should be balanced before we can proceed with the trade linking procedure.

In order to balance the OECD IO tables we make use of the nonlinear programming techniques and formulate the following system of equations:

1. Supply is equal demand for each commodity
2. No re-exports: total domestic output times 0.9 should be not lower than the total exports per type of commodity
3. No re-imports: the total consumption in basic prices should be not lower than the total imports per type of commodity
4. The elements of the IO table (with the exception of changes in inventories, exports and imports) should not deviate with more than 5% from the initial scaled up to 2013 version of the IO tables.

The distance from the initial scaled up to 2013 version of IO tables and the outcomes of the nonlinear programming problem measured as the entropy function is minimized under the system of equations presented above.

### 2.3.2 Consistent disaggregation of Supply and Use Tables for 2013 to NACE Rev2 sectoral and commodity classification

In order to be able to use the OECD data in the trade linking procedure we need to disaggregate the OECD IO tables to the level of details of the Eurostat SUTs that is to the level of details of NACE Rev2 sectoral and commodity classification. This is done using the mapping that we have prepared between the OECD and Eurostat classifications. The OECD classification is quite similar to the NACE Rev1 and we have made use of the mappings between NACE Rev1 and Rev2 that are available from Eurostat-RAMON (<http://ec.europa.eu/eurostat/ramon> ).

In order to disaggregate the OECD IO tables to the format and sectoral/commodity classification of the Eurostat SUTs we have taken the following steps:

1. For each OECD country identify a 'similar' EU28 country which economic sectoral and technological (sectoral inputs) structure will be used for disaggregation.
2. Construct Supply and Use tables on the basis of OECD IO tables where the supply is diagonal. For the construction of use tables we make use of transport and trade margins and net taxes ratios from the 'similar' EU28 country in order to go from producer/basic to consumer prices (IO tables are given in producer/basic prices and need to be translated into consumer prices using information on transport and trade margins and net taxes).
3. Disaggregate different parts of the constructed OECD SUTs using the data from Eurostat SUTs taking into account the inconsistencies. If there is no data from Eurostat SUTs available, the disaggregation is done proportionally between the number of sectors and commodities that are mapped to the OECD aggregated commodity/sector groups.
4. Solve the nonlinear programming problem that includes equations and optimization function described in section 2.2 in combination with the restrictions that ensure that the disaggregate OECD SUTs sum up to the initial balanced OECD IO tables with the exception of changes in inventories element of the IO tables. In making the correct relationships one should take into account that the use table is in consumer prices and the IO table in in the basic prices. The layers of trade and transport margins and net taxes on consumptions should be used in the equations in order to ensure the consistency.

The outcome of this procedure is the set of SUTs for all the countries and rest of the world regions of the OECD dataset.

**Table 7 The list of countries in the global OECD IO database**

Australia	AUS	Israel	ISR	Switzerland	CHE	India	IND
Austria	AUT	Italy	ITA	Turkey	TUR	Indonesia	IDN
Belgium	BEL	Japan	JPN	United Kingdom	GBR	Latvia	LVA
Canada	CAN	Korea	KOR	United States	USA	Lithuania	LTU
Chile	CHL	Luxembourg	LUX	Argentina	ARG	Malaysia	MYS
Czech Republic	CZE	Mexico	MEX	Brazil	BRA	Malta	MLT
Denmark	DNK	Netherlands	NLD	Brunei Darussalam	BRN	Philippines	PHL
Estonia	EST	New Zealand	NZL	Bulgaria	BGR	Romania	ROU
Finland	FIN	Norway	NOR	Cambodia	KHM	Russia	RUS
France	FRA	Poland	POL	China (Peoples Republic of)	CHN	Saudi Arabia	SAU
Germany	DEU	Portugal	PRT	Colombia	COL	Singapore	SGP
Greece	GRC	Slovak Republic	SVK	Costa Rica	CRI	South Africa	ZAF
Hungary	HUN	Slovenia	SVN	Croatia	HRV	Chinese Taipei	TWN
Iceland	ISL	Spain	ESP	Cyprus	CYP	Thailand	THA
Ireland	IRL	Sweden	SWE	Hong Kong, China	HKG	Tunisia	TUN
						Viet Nam	VNM
						Rest of the world	ROW

## 2.4 Linking Supply and Use tables with inter-national trade flows

### 2.4.1 Adjusting the trade flows from BACI database for re-exports

The BACI and UN trade in services datasets provide us with the necessary data on the international trade flows in both goods and services in 2013. One of the difficulties of using the BACI dataset is the treatment of re-exports and re-imports in it. For the construction of BACI CEPII has used all the available data on re-exports and re-imports from UN COMTRADE (this has been verified in the personal communications with the colleagues at CEPII). Unfortunately such data was available for many non-European countries but not the EU28 countries including the typical re-export countries such as the Netherlands, the UK, Luxemburg and Belgium.

This means that the BACI trade flows should be adjusted for the re-exports and re-imports in cases of the EU28 countries and not in case of non-European countries. At the previous steps of the data analysis we have been adjusting the SUTs and IO tables for re-exports and re-imports which has resulted in the values of re-exports and re-imports being calculated per country and per type of good and service. The adjustment procedure that has been implemented can be described as follows:

1. Calculate the trade flows that correspond to the re-exports of the country  $cntt$  by allocating them to the correct origin and destination countries  $cnt$  and  $cntt$  respectively following the patterns of incoming and outgoing trade flows of the country  $cntt$ . The following formula calculates the re-exports of country  $cntt$  that actually represent the trade between the countries  $cnt$  and  $cnttt$ :

$$Re\_flows_{cnt,cntt,cnttt,p} = -Re\ exports_{cntt,p} \cdot \frac{Trade_{cnt,cntt,p}}{\sum_{cnttt} Trade_{cnttt,cntt,p}} \cdot \frac{Trade_{cntt,cnttt,p}}{\sum_{cnttt} Trade_{cntt,cnttt,p}} \quad (8)$$

2. The initial value of trade between the countries is increased with the value of the additional trade flows that represent the re-exports of the EU28 countries:

$$Trade_{cnt,cntt,p} = Trade_{cnt,cntt,p} + \sum_{cnttt} Re\_flows_{cnt,cnttt,cntt,p} \quad (9)$$

This adjusted value of trade flows is used for the calculation of the trade shares and trade flows consistent with the values in the SUTs.

Before starting the trade-linking procedure we should make sure that the global values of exports and imports are consistent, that is if there are exports of particular good or service from one of the countries of the world than there should also exist imports of this good or service by one of the countries. The checks show that this is not the case for some types of services, which means that their values of exports/imports in the SUTs should be put to zero in order to avoid inconsistencies in the trade linking procedure.

We have also found the following inconsistencies between the international trade data, data on bi-lateral trade and transport margins (based on BACI) and the data on exports and imports from the SUTs:

1. There is data on exports or imports in the SUTs but there is no corresponding trade flows data: in this case we have used the data on exports or imports of other countries in order to split the SUTs data between possible origins and destinations and this way create the data on the missing trade flows.
2. There is data on trade flows but there is no corresponding data on exports or imports in the SUTs: in this case we have removed the data on trade flows as for us the leading (or priority) data is the data from the SUTs.
3. There is data on trade flows for goods but there is no corresponding data on bi-lateral trade and transport margins: in this case we have created the trade and transport margins between these origin and destination countries as the average of the existing trade and transport margin data for other types of goods traded between these two countries.

### 2.4.2 Using nonlinear programming to find the trade flows between the countries

The following nonlinear programming problem has been solved in order to create the trade flows between the EU28 and other non-European countries of the world. The trade system is a closed one and covers the whole world.

Sets are defined as:

- *TTmargin* trade and transport margins
- 

Variables are defined as:

- *Trade\_v<sub>cnt,cntt,p</sub>* inter-national trade
- *TT\_margin\_v<sub>cnt,cntt,p</sub>* inter-national trade and transport margins
- *Exports\_v<sub>cnt,p</sub>* total country exports
- *Imports\_v<sub>cnt,p</sub>* total country imports
- *Inventories\_v<sub>cnt,p</sub>* changes in inventories

Equations are defined as:

- Exports of the country are equal to the sum of outgoing trade flows in FOB prices:

$$Exports\_v_{cnt,p} = \sum_{cntt} Trade\_v_{cnt,cntt,p} \quad (10)$$

- Imports of the country are equal to the sum of incoming trade flows in CIF prices (that is including trade and transport margins):

$$Imports\_v_{cnt,p} = \sum_{cntt} Trade_{cntt,cnt,p} \cdot (1 + TT\_margin\_v_{cntt,cnt,p}) \quad (11)$$

- The total international trade in transport and trade related services is equal to the total value of the inter-national trade and transport margins:

$$\sum_{cnt,cntt,p \in TTmargin} Trade_{cnt,cntt,p} = \sum_{cnt,cntt,p} Trade_{cnt,cntt,p} \cdot TT\_margin\_v_{cnt,cntt,p} \quad (12)$$

- Minimized the distance (measured as entropy) between the initial estimates of the trade flows based on international trade data (BACI and UN trade in services) and the outcomes of the nonlinear programming problem:

$$\sum_{cnt,cnt,p} Trade_{cnt,cnt,p} \cdot \log\left(Trade_{cnt,cnt,p} / Trade_{cnt,cnt,p}\right) \rightarrow \min \quad (13)$$

# 3 Regionalization of country level Supply and Use Tables

## 3.1 Overview of regional-level data for EU28

The regionalization of the national level Supply and Use tables makes use of several statistics available from Eurostat and other publicly available data sources. These used data sources are presented in Table 8 below.

**Table 8: Overview of the available data sources at NUTS2 level for EU28**

<b>Data source</b>	<b>Availability</b>	<b>Sectoral/commodity details</b>	<b>Geographical details</b>	<b>Notes</b>
<b>Eurostat regional accounts – GDP, households’ incomes, employment and wages</b>	2000-2013	14 NACE Rev2 sectors (cover the whole economy)	NUTS1 2010 and NUTS2 2010 regions of EU28 + NO + CH + IS + MK + TR	Some of the sectors are the aggregates of the sub-sectors
<b>Eurostat SBS – employment and wages</b>	2000-2011	100 NACE Rev2 sectors (cover industry and private services)	NUTS1 2010 and NUTS2 2010 regions of EU27 (no HR ) + NO	Some of the sectors are the aggregates of the sub-sectors
<b>ETIS-Plus database (freight and passenger transport flows by mode; survey based source data)</b>	2000 and 2010	Freight flows in NST2 classification (52 types of goods)  Passenger trips by 7 transport modes, 4 trips lengths, differentiated between business, private, vacation and commuting  International trade in values and in volumes	NUTS1 2006, NUTS2 2006 and NUTS3 2006 regions of EU28 (in total for 235 countries of the world by sub-national regions of these countries)	This database has been constructed for DG MOVE and is used as the baseline database of the TRANSTOOLS model  Freight flows between the regions are represented in volumes

Data from regional accounts consists of the information on wages and employment by NACE Rev2 economic sectors according to the classification presented in Table 9. This sectoral level of detail is not very detailed but covers the whole of the economy. Regional accounts data does not have any missing values and hence is fully complete.

**Table 9 Sectoral classification of the regional accounts data at NUTS2 level**

A	Agriculture, forestry and fishing
<b>B-E</b>	<b>Industry (except construction)</b>
C	Manufacturing
F	Construction
<b>G-J</b>	<b>Wholesale and retail trade; transport; accommodation and food service activities; information and communication</b>
G-I	Wholesale and retail trade, transport, accommodation and food service activities
J	Information and communication
<b>K-N</b>	<b>Financial and insurance activities; real estate activities; professional, scientific and technical activities; administrative and support service a...</b>
K	Financial and insurance activities
L	Real estate activities
M_N	Professional, scientific and technical activities; administrative and support service activities
<b>O-U</b>	<b>Public administration and defence; compulsory social security; education; human health and social work activities; arts, entertainment and recreati...</b>
O-Q	Public administration, defence, education, human health and social work activities
R-U	Arts, entertainment and recreation; other service activities; activities of household and extra-territorial organizations and bodies

Another set of sectoral data at the NUTS2 regional level provided by Eurostat are the Structural Business Statistics (SBS) dataset. This dataset provides much more sectoral details at NACE Rev2 classification for the private part of the economic sectors and includes information on both wages and employment. The level of sectoral details is presented at Table 10. The SBS dataset has some missing values for some regions and sectors that we have imputed using the data on regions with similar levels of GDP per capita. In several cases we used SBS data from earlier years to fill in gaps. The share of missing values in the SBS dataset is less than 1% of all observations.

In order to be able to regionalize the 65 NACE Rev2 sectors of the Supply and Use tables we have chosen to combine the data from SBS and regional accounts. SBS data is used for the regionalization of private economic sectors and regional accounts dataset is used for regionalization of agriculture, forestry and fishery as well as public economic sectors.





**Table 10 Sectoral details of the Structural Business Statistics data from Eurostat**

<b>B</b>	<b>Mining and quarrying</b>	C23	Manufacture of other non-metallic mineral products	F42	Civil engineering	G473	Retail sale of automotive fuel in specialised stores	J61	Telecommunications
B05	Mining of coal and lignite	C24	Manufacture of basic metals	F43	Specialised construction activities	G474	Retail sale of information and communication equipment in specialised stores	J62	Computer programming, consultancy and related activities
B06	Extraction of crude petroleum and natural gas	C25	Manufacture of fabricated metal products, except machinery and equipment	<b>G</b>	<b>Wholesale and retail trade; repair of motor vehicles and motorcycles</b>	G475	Retail sale of other household equipment in specialised stores	J63	Information service activities
B07	Mining of metal ores	C26	Manufacture of computer, electronic and optical products	<b>G45</b>	<b>Wholesale and retail trade and repair of motor vehicles and motorcycles</b>	G476	Retail sale of cultural and recreation goods in specialised stores	<b>L</b>	<b>Real estate activities</b>
B08	Other mining and quarrying	C27	Manufacture of electrical equipment	G451	Sale of motor vehicles	G477	Retail sale of other goods in specialised stores	L68	Real estate activities
B09	Mining support service activities	C28	Manufacture of machinery and equipment n.e.c.	G452	Maintenance and repair of motor vehicles	G478	Retail sale via stalls and markets	<b>M</b>	<b>Professional, scientific and technical activities</b>
<b>C</b>	<b>Manufacturing</b>	C29	Manufacture of motor vehicles, trailers and semi-trailers	G453	Sale of motor vehicle parts and accessories	G479	Retail trade not in stores, stalls or markets	M69	Legal and accounting activities
C10	Manufacture of food products	C30	Manufacture of other transport equipment	G454	Sale, maintenance and repair of motorcycles and related parts and accessories	<b>H</b>	<b>Transportation and storage</b>	M70	Activities of head offices; management consultancy activities
C11	Manufacture of beverages	C31	Manufacture of furniture	<b>G46</b>	<b>Wholesale trade, except of motor vehicles and motorcycles</b>	H49	Land transport and transport via pipelines	M71	Architectural and engineering activities; technical testing and analysis
C12	Manufacture of tobacco products	C32	Other manufacturing	G461	Wholesale on a fee or contract basis	H50	Water transport	M72	Scientific research and development
C13	Manufacture of textiles	C33	Repair and installation of machinery and equipment	G462	Wholesale of agricultural raw materials and live animals	H51	Air transport	M73	Advertising and market research
C14	Manufacture of wearing apparel	<b>D</b>	<b>Electricity, gas, steam and air conditioning supply</b>	G463	Wholesale of food, beverages and tobacco	H52	Warehousing and support activities for transportation	M74	Other professional, scientific and technical activities
C15	Manufacture of leather and related products	D35	Electricity, gas, steam and air conditioning supply	G464	Wholesale of household goods	H53	Postal and courier activities	M75	Veterinary activities

C16	Manufacture of wood and of products of wood and cork, except furniture; manufacture of articles of straw and plaiting materials	E	<b>Water supply; sewerage, waste management and remediation activities</b>	G465	Wholesale of information and communication equipment	I	<b>Accommodation and food service activities</b>	N	<b>Administrative and support service activities</b>
C17	Manufacture of paper and paper products	E36	Water collection, treatment and supply	G466	Wholesale of other machinery, equipment and supplies	I55	Accommodation	N77	Rental and leasing activities
C18	Printing and reproduction of recorded media	E37	Sewerage	G467	Other specialised wholesale	I56	Food and beverage service activities	N78	Employment activities
C19	Manufacture of coke and refined petroleum products	E38	Waste collection, treatment and disposal activities; materials recovery	G469	Non-specialised wholesale trade	J	<b>Information and communication</b>	N79	Travel agency, tour operator reservation service and related activities
C20	Manufacture of chemicals and chemical products	E39	Remediation activities and other waste management services	<b>G47</b>	<b>Retail trade, except of motor vehicles and motorcycles</b>	J58	Publishing activities	N80	Security and investigation activities
C21	Manufacture of basic pharmaceutical products and pharmaceutical preparations	F	<b>Construction</b>	G471	Retail sale in non-specialised stores	J59	Motion picture, video and television programme production, sound recording and music publishing activities	N81	Services to buildings and landscape activities
C22	Manufacture of rubber and plastic products	F41	Construction of buildings	G472	Retail sale of food, beverages and tobacco in specialised stores	J60	Programming and broadcasting activities	N82	Office administrative, office support and other business support activities

In order to disaggregate EU28 Supply and Use (SUTs) tables from the national to regional NUTS2 level we use the regional-level indicators specific for each element of the Supply and Use tables. In some cases these indicators are Eurostat data such as regional sectoral wages and regional GDP whereas in other cases the indicators are derived on the basis of other regionalized elements of the SUTs. Table 11 presents the mapping between the indicators used for regionalization and the separate elements of the SUTs. Unfortunately, there is not always a direct proxy available for the regionalization of the different columns or rows in the SUTs. In those case we used an available indirect proxy derived from economic theory. Please note that a proxy like “Total regional intermediate inputs by type of good/service” can only be determined after the sector columns for the regions have been regionalized.

**Table 11 Mapping between the elements of national-level Supply and Use tables and the regional data at NUTS2 level from Eurostat**

<b>Element of the national –level Supply and Use tables</b>	<b>Data at the regional NUTS2 level from Eurostat used for regionalization/disaggregation</b>	<b>Derived indicator used for regionalization/disaggregation</b>
<b><i>Intermediate demand/sectoral inputs</i></b>	Wage sum by region and sector	GDP based on national capital share and total regional GDP data
<b><i>Sectoral outputs</i></b>	Wage sum by region and sector	GDP based on national capital share and total regional GDP data
<b><i>Final consumption expenditure of households and NPISH</i></b>	Households’ income	Not applicable
<b><i>Final consumption expenditure of NPISH</i></b>	Households’ income	Not applicable
<b><i>Final consumption expenditure of government</i></b>	Households’ income	Not applicable
<b><i>Gross fixed capital formation</i></b>	Not available	Total regional intermediate inputs by type of good/service
<b><i>Taxes less subsidies on products</i></b>	Not available	Total regional production for region use by type of good/service
<b><i>Trade and transport margins</i></b>	Not available	Total regional consumption by type of good/service
<b><i>Compensation of employees</i></b>	Wage sum by region and sector	GDP based on national capital share and total regional GDP data
<b><i>Other net taxes on production</i></b>	Wage sum by region and sector	GDP based on national capital share and total regional GDP data
<b><i>Consumption of fixed capital</i></b>	Wage sum by region and sector	GDP based on national capital share and total regional GDP data
<b><i>Operating surplus net</i></b>	Wage sum by region and sector	GDP based on national capital share and total regional GDP data
<b><i>Changes in inventories and valuables</i></b>	Not available	Total regional consumption by type of good/service

The formula used for regionalization of the national elements of the SUTs is presented below:

$$X_r = Y_l \cdot \frac{I_r}{\sum_{k \in S_l} I_k}$$

where  $X_r$  is the element of regional SUTs of region  $r$ ,  $Y_l$  is the corresponding element of the national SUTs of country  $l$ ,  $I_r$  is the used indicator,  $S_l$  is the set of NUTS2 regions of country  $l$ , indexes  $r, k$  are used for regions and index  $l$  is used for countries. The disaggregation formulas are used for all elements of the SUTs except for the changes in inventories and valuables.

Table 12 below presents various categories of Eurostat Supply and Use tables and their corresponding codes that are important for the regionalization. These codes are used in the formula for the derivation of regional-level changes in inventories and valuables.

**Table 12 Sub-Category of the Supply and Use tables with Eurostat codes**

Name of the SUTs category	Code
Final consumption expenditure by households	P3_S14
Final consumption expenditure by non-profit organisations serving households (NPISH)	P3_S15
Final consumption expenditure by government	P3_S13
Gross fixed capital formation	P51
Changes in inventories and valuables	P52_P53
Gross capital formation	P5
Exports FOB	P6
Compensation of employees	D1
Other net taxes on production	D29_M_D39
Consumption of fixed capital	K1
Operating surplus, net	B2N_B3N
Imports CIF	P7
Trade and transport margins	P118
Taxes less subsidies on products	D21_M_D31
Net trade of a region with the rest of the country	T1

On the regional level we introduced one extra column in the use table. This column are the region and product specific net trade of the region with the rest of the country. This regional-level net trade at product level  $p$  is calculated as:

$$USE_{p,T1} = \sum_c SUP_{p,c} - \sum_s USE_{p,s} - USE_{p,P3\_S13} - USE_{p,P3\_S14} - USE_{p,P3\_S15} - USE_{p,P51} - USE_{p,P6} - USE_{p,P52\_P53}$$

where  $c$  is the index for the columns, and  $s$  is the index for the economic sectors.

## 1.1. Deriving inter-regional trade flows

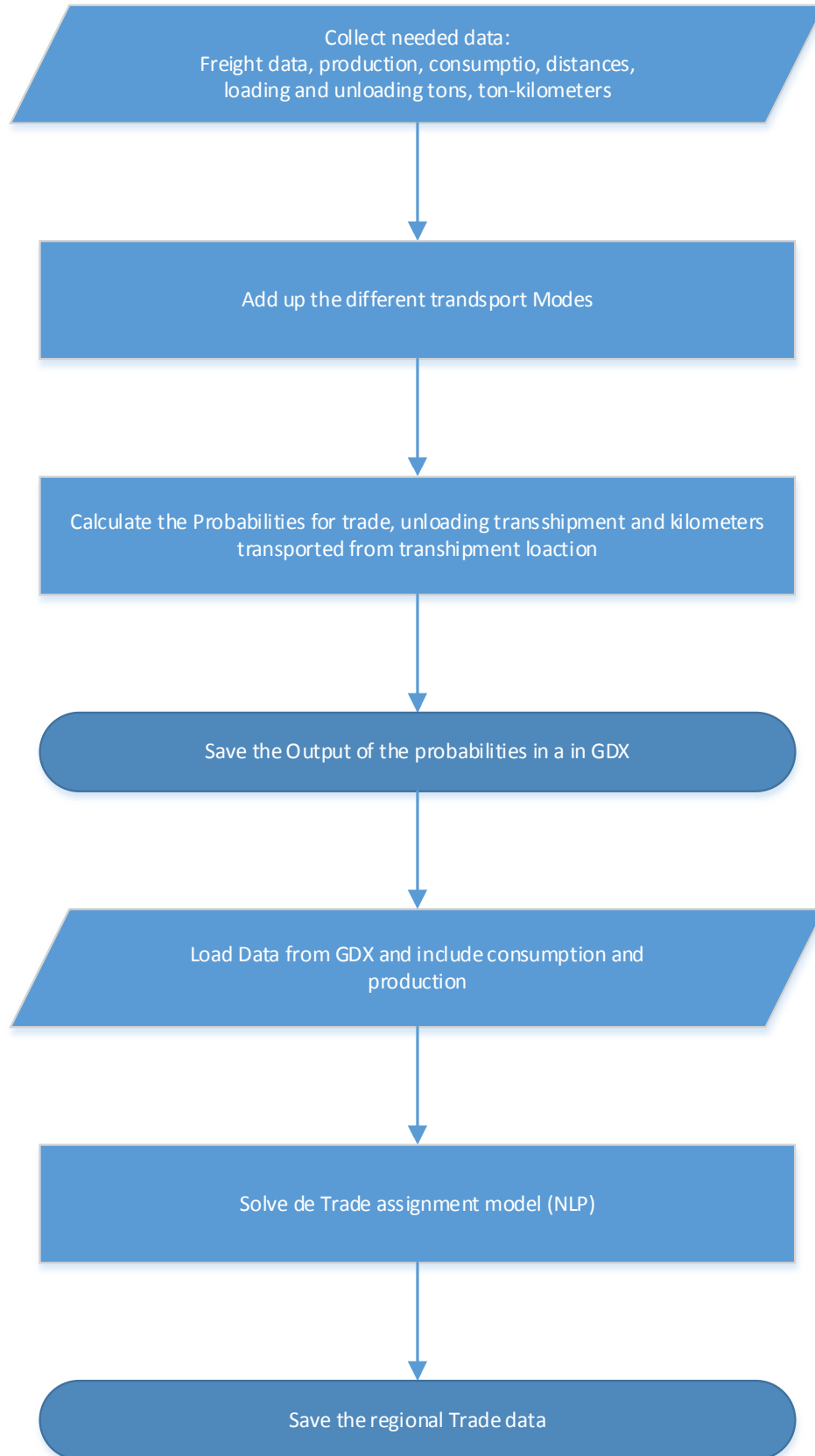
In order to determine the interregional trade between NUTS2 regions and between NUTS2 regions and the rest of the world we use a newly developed estimation technique. We determine the trade between nuts2 regions given data on freight transport and regionalized supply and use tables for the European NUTS2 regions. The methodology is based on linear and non-linear optimization techniques. The methodology consists of two independent steps. In the first step we determine the probability matrices of trade between regions using 0, 1, 2, 3 or 4 transshipment locations. In the second step these probability matrices are used to estimate the trade between the regions where we minimize the estimate for value per ton shipped in a country and the data on ton goods leaving a region.

The end result is a regional trade matrix that is not only consistent with the regional supply and use tables, but also stays as close as possible to the main European transport data. The associated transport matrix estimated simultaneously with the trade flows represent the complete chain of multimodal transport (5 modes) with endogenously determined transshipment locations from a region where the product\service is produced to a region where the product\service is consumed.

The estimation of the inter-regional trade flows is schematically presented in Figure 2. In Figure 2 we see that the estimation methodology of the regional trade consists of two main parts: the calculation of different probabilities of trade between regions and associated information like ton-kilometers transported and the estimation of these trade flows based on these probabilities. All data is used in gams data files (gdx) for matter of convenience since all programs have been written in gams.

Trade in services is estimated in a comparable way to the trade in goods. However, now business travel is used as a proxy for trade relations ships. Also business travelers use multiple modes and these stopovers are therefore taken into account like transshipments for the transport of goods.

**Figure 2: Procedure followed to estimate regional trade**



### 3.1.1 Distribution Probabilities

In order to calculate all possible trade destinations for different number of transshipment transport of the goods we need probability matrices for goods using different amounts of transshipment  $\tau$ . We consider up to 5 transshipments. The basis is the probability matrix  $\chi_{\tau,p,r,s}$  without transshipment that is derived from the freight matrix  $F_{p,r,s}$  as follows.

$$\chi_{0,p,r,s} = \frac{F_{p,r,s}}{\sum_{s'} F_{p,r,s'}} \quad (14)$$

Where  $r$  and  $s$  are origin and destination nuts2 regions.

Using the  $\xi_{r,s}$  Distance matrix in km from region  $r$  to region  $s$  we can also determine the following associated distance  $\zeta_{0,p,r,r}$  for non-transshipment trade.

$$\begin{aligned} \zeta_{0,p,r,r} &= \sum_s \chi_{0,p,r,s} \xi_{r,s} \\ \psi_{0,p,r,r} &= 1 \end{aligned} \quad (15)$$

Where  $\psi_{\tau,p,r,s}$  is the probability matrix of trade of product  $p$  from region  $r$  that will be transshipped in region  $s$  and that is using  $\tau$  transshipment locations.

Using this information we can determine the probability of trade using one or multiple transshipment locations. The following set of equations therefore determines the needed probabilities and distances.

$$\begin{aligned} \chi_{1,p,r,s} &= \sum_{r'|r' \neq r, r' \neq s} \chi_{0,p,r,r'} \chi_{0,p,r',s} \\ \zeta_{1,p,r,r'} &= \sum_{s|r' \neq r, r' \neq s} \chi_{0,p,r,r'} \chi_{0,p,r',s} \xi_{r,s} \\ \psi_{1,p,r,r'} &= \sum_{s|r' \neq r, r' \neq s} \chi_{0,p,r,r'} \chi_{0,p,r',s} = \chi_{0,p,r,r'} \end{aligned} \quad (16)$$

There is one more condition on  $r'$  that is left out of the above equation. This condition is that if  $r'$  is in a different country than  $r$ , then  $r$  is also in a different country than  $s$ . In a comparable way all parameters for the different number of transshipment trade are determined.

We also need the probabilities of a good leaving a region for every transshipment route and we also need the kilometers of these good leaving that region. These probabilities can be easily calculated from the probabilities of transshipment summing up in different points of the transport chain.

### 3.1.2 Trade assignment Models

Let us have regions  $r, s$ , countries  $l, k$  and products  $p$ . Trade is estimated to minimize the error on the data available. The objective function is a weighted minimization of the quadratic relative and absolute error. Production  $X_{p,r}$  is the sum over the trade matrix in producer prices, while consumption  $C_{p,s}$  in consumer prices is the sum over the trade added with the trade and transport margins. Trade  $H_{p,r,s}$  can be transported using  $\tau [0, \dots, 4]$  transshipment locations. Notice that the model cannot be solved for all products separately since they are dependent on each other with respect to data on total loading, unloading and ton kilometers. It is assumed that the value per ton transported for a good is comparable in neighboring regions. Therefore a weighted error is specified according to equation 1.5 below, where  $\bar{\xi}$  is the average distance between all regions. The errors in the estimation are described as  $\varepsilon$  with the name of the variable the error is related to. Thus,  $\varepsilon_V$  is the error related to the value per ton estimate.

### The Trade Estimation Model

$$\text{Minimize } Z = \sum_{p,r,s} \left( H_{p,r,s} - \sum_{\tau} Q_{\tau,p,r} \chi_{\tau,p,r,s} \right)^2 + \sum_{\tau,p,r} \left( \varepsilon q_{\tau,p,r}^2 \right) \\ + \sum_{p,r} \left( \varepsilon v_{p,r}^2 + \varepsilon u_{p,r}^2 + \varepsilon n_{p,r}^2 \right) + \sum_r \left( \varepsilon ut_r^2 + \varepsilon nt_r^2 \right)$$

Subject to

$$1 = \sum_s H_{p,r,s}$$

$$C_{p,s} = \sum_r (1 + \mu_{r,s}) H_{p,r,s} X_{p,r}$$

$$T_{p,l,k} = \sum_{r \in l, s \in k} H_{p,r,s} X_{p,r}$$

$$\varepsilon v_{p,r} = \sqrt{\frac{\bar{\xi}}{\xi_{r,s}}} (v_{p,r} - v_{p,s})$$

$$\varepsilon q_{\tau,p,r} = \sqrt{\frac{\bar{\xi}}{\xi_{r,s}}} (Q_{\tau,p,r} - Q_{\tau,p,s})$$

$$\varepsilon ut_s \geq 1 - \frac{\sum_r \left( \sum_{\tau,r} Q_{\tau,p,r} \chi_{\tau,p,r,s} + \sum_{\tau,r \neq s} Q_{\tau,p,r} \psi_{\tau,p,r,s} \right)}{\bar{U}t_s}$$

$$\varepsilon nt_r \geq 1 - \frac{\sum_r \sum_{\tau,s} Q_{\tau,p,r} \psi_{\tau,p,r,s}}{\bar{N}t_p}$$

$$\varepsilon u_{p,s} \geq 1 - \frac{\left( \sum_{\tau,r} Q_{\tau,p,r} \chi_{\tau,p,r,s} + \sum_{\tau,r \neq s} Q_{\tau,p,r} \psi_{\tau,p,r,s} \right)}{\bar{U}_{p,s}}$$

$$\varepsilon n_{p,r} \geq 1 - \frac{\sum_{\tau,s} Q_{\tau,p,r} \psi_{\tau,p,r,s}}{\bar{N}_{p,r}}$$

$$\varepsilon g_s \geq 1 - \frac{\sum_{\tau,p,r} Q_{\tau,p,r} \psi_{\tau,p,r,s} \zeta_{\tau,p,r,s}}{\bar{G}_s}$$

$$\varepsilon u_{p,s} \geq 0; \varepsilon n_{p,r} \geq 0; \varepsilon g_{p,s} \geq 0$$



**Exogenous Variables and parameters needed for probabilities**

$F_{p,r,s}$  Freight of product  $p$  from region  $r$  to region  $s$  in tons

$\xi_{r,s}$  Distance matrix in km from region  $r$  to region  $s$

**Exogenous Variables and parameters Trade Estimation**

$X_{p,r}$  total production of product  $p$  in region  $r$  in values

$C_{p,r}$  consumption of product  $p$  in region  $r$  in values

$\chi_{\tau,p,r,s}$  probability matrix of trade of product  $p$  from region  $r$  to region  $s$  that is going to be traded using  $\tau$  transshipment locations

$\psi_{\tau,p,r,s}$  probability matrix of trade of product  $p$  from region  $r$  that will be transshipped in region  $s$  and that is using  $\tau$  transshipment locations

$\zeta_{\tau,p,r,s}$  Distance matrix in km of trade of product  $p$  from region  $r$  that is using  $\tau$  transshipment locations and is leaving transshipment region  $s$

$T_{p,l,k}$  Country trade of product  $p$  from country  $l$  to country  $k$

$\bar{U}_{p,r}$  Data on Goods unloaded in region  $r$  (tons)

$\bar{N}t_r$  Data on Goods loaded in region  $r$  (tons)

$\bar{U}t_r$  Data on Goods unloaded in region  $r$  (tons)

$\bar{N}_{p,r}$  Data on Goods loaded in region  $r$  (tons)

$\bar{G}_r$  Data on Ton kilometers of goods leaving region  $r$

**Endogenous positive Variables Trade Estimation**

$Q_{\tau,p,r}$  production of product  $p$  in region  $r$  in tons that is going to be traded using  $\tau$  transshipment locations

$v_{p,r}$  Value per ton

$G_{p,r}$  Ton kilometers of goods leaving region  $r$  (tons)

The trade assignment model estimating the trade in services is the same as the model used to estimate the trade in goods. The only difference is that the probability matrices are based on business traveler trips, and that these business travelers are supposed to have no more than 2 stopovers. The transport services are estimated using only the objective function of the quadratic distance between the estimated and the predicted trade in transport services (the prior). This predicted trade is assumed to be proportional to the export of goods leaving the region. It is therefore implicitly assumed that the exporting region will pay for the transport services needed to export the goods.

# 4 Results

The methodology results in a set of supply and use tables at the EU28 nuts2 regions. The detailed supply and use tables can be aggregated to the level of aggregation needed in the modelling exercises with the Rhomolo model. The regional trade matrices that accompany these tables are not only consistent with the regional supply and use tables, but also with the main European transport data taking multimodal transport (5 modes) with endogenously determined transshipment locations into account. This makes it possible to analyse the importance of transshipment locations (hubs) in regional trade and link up actual transport costs to multiregional trade flows.

The results are difficult to assess or analyse due to the size of the dataset and its region and sector specific economic structure and trade patterns. Below we focus therefore on one of the key variables in the estimation: the average amount of times a good is transhipped before it reaches its location. This variable gives a good indication of the importance of the used methodology and the validity of other methods that are based on gravity equation estimation using transport data. In the case of many transhipped goods such gravity estimation is based on the “wrong” trade links and will therefore give erroneous trade estimates.

We present the average number of transshipment per type of good in Table 12 with t-values in between brackets. What we see is that the estimates are very stable over the regions with high t-values. In other words, the variation in the number of transshipments depends on the type of good and not on the region of origin. We find that many bulked goods are hardly transhipped, while fabricated goods are transhipped many times.

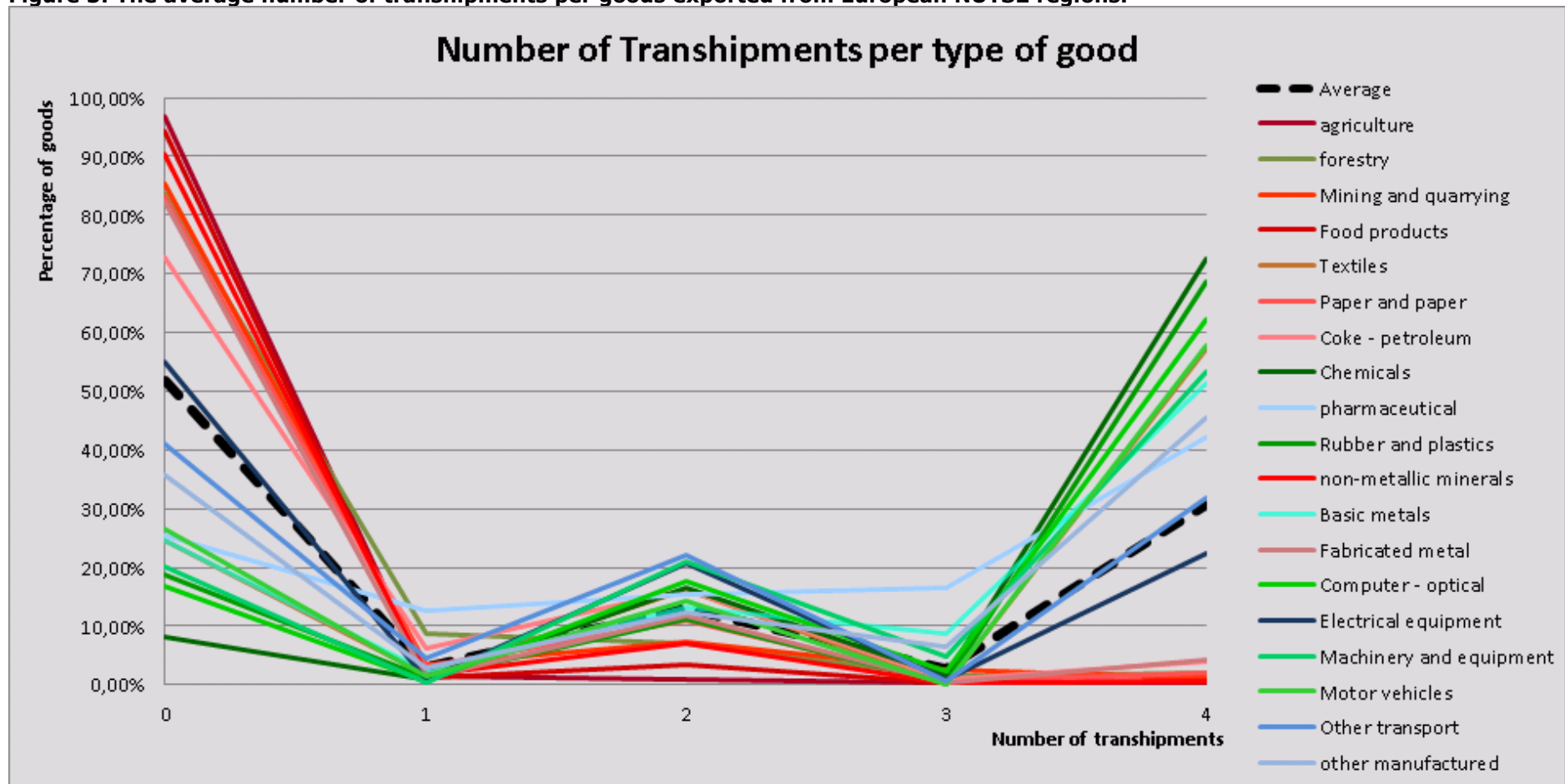
This dichotomy becomes more visible when we present the same results in Figure 3. In Figure 3 we see clearly that only goods like agricultural products, mining, food and oil directly reaches their final destination without transshipments. This implies that using a gravity model to estimate trade based on transport data is only possible for these type of bulk goods. All other goods cannot be estimated in the same way since they are transhipped many times.

The new methodology outperforms therefore gravity equation based estimations based on transport data. The trade estimate improves with more detailed information transported goods is being used. This strengthens the validity of the trade dataset and extends the use of the data beyond the field of economics (i.e. transport and logistics). The goods trade estimates are more detailed due to improved quality of micro data on freight transport and the improved data on regional business travel will result in better services trade estimates. Moreover, improved estimation of the amount of cross-hauling will be achieved by integrating this in the estimation methodology.

**Table 13: The average number of transshipments per goods exported from European Nuts2 regions.**

Transshipments	0	(t)	1	(t)	2	(t)	3	(t)	4	(t)
Average	0,52		0,03		0,13		0,03		0,31	
Agriculture	0,97	(187)	0,02	(6)	0,01	(5)	0,00	(3)	0,00	(2)
Forestry	0,84	(408)	0,09	(17)	0,07	(14)	0,01	(3)	0,02	(4)
Mining and quarrying	0,85	(104)	0,03	(11)	0,07	(13)	0,03	(10)	0,01	(6)
Food products	0,94	(239)	0,01	(11)	0,04	(12)	0,00	(5)	0,01	(5)
Textiles	0,25	(155)	0,02	(36)	0,16	(86)	0,00	(6)	0,57	(405)
Paper and paper	0,83	(324)	0,03	(42)	0,11	(51)	0,01	(8)	0,02	(15)
Coke - petroleum	0,73	(159)	0,06	(31)	0,16	(46)	0,01	(8)	0,04	(18)
Chemicals	0,08	(55)	0,01	(18)	0,16	(74)	0,02	(22)	0,73	(372)
pharmaceutical	0,25	(31)	0,13	(13)	0,15	(17)	0,17	(18)	0,42	(66)
Rubber and plastics	0,19	(119)	0,01	(31)	0,11	(82)	0,00	(6)	0,69	(497)
non-metallic minerals	0,90	(164)	0,02	(12)	0,07	(15)	0,00	(4)	0,01	(5)
Basic metals	0,25	(157)	0,02	(32)	0,13	(58)	0,09	(80)	0,51	(191)
Fabricated metal	0,82	(338)	0,01	(23)	0,12	(64)	0,00	(5)	0,04	(23)
Computer - optical	0,17	(134)	0,01	(19)	0,18	(156)	0,02	(45)	0,62	(455)
Electrical equipment	0,55	(398)	0,01	(23)	0,21	(130)	0,01	(22)	0,23	(156)
Machinery and equipment	0,20	(166)	0,00	(9)	0,21	(113)	0,05	(54)	0,53	(364)
Motor vehicles	0,26	(178)	0,01	(34)	0,14	(120)	0,00	(8)	0,58	(402)
Other transport	0,41	(144)	0,05	(47)	0,22	(105)	0,01	(14)	0,32	(108)
other manufactured	0,36	(95)	0,03	(6)	0,12	(25)	0,07	(13)	0,45	(143)

**Figure 3: The average number of transhipments per goods exported from European NUTS2 regions.**



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